10.2 The Fundamental Theorem of Calculus

Indefinite Integral –

$$\int 2x \, dx =$$

Definite Integral –

$$\int_{1}^{3} 2x dx =$$

$$\int_{0}^{\frac{\pi}{2}} \cos x \, dx = \int_{-2}^{1} 5z^2 - 7z + 3 \, dz = \int_{1}^{4} \frac{8}{\sqrt{t}} - 12\sqrt{t^3} dt =$$

Properties of Definite Integrals –

$$\int_{a}^{a} f(x)dx = 0 \qquad \qquad \int_{a}^{b} f(x)dx = -\int_{b}^{a} f(x)dx$$

The definite integral of f from a to b is defined by:

$$\int_{a}^{b} f(x)dx = \lim_{n \to +\infty} \sum_{k=1}^{n} f(x_k) \Delta x$$

The Fundamental Theorem of Calculus (part 1)

If f is continuous on the interval [a, b], then

$$\int_{a}^{b} f(x)dx = F(b) - F(a)$$
where F is any antiderivative of f.

Find the <u>exact</u> area beneath the curve $y = x^2 + 1$ from x = 0 to x = 3

The Fundamental Theorem of Calculus (part 2) –